

## AP® BIOLOGY EQUATIONS AND FORMULAS

Statistical Analysis and Probability																																				
<p><b>Mean</b></p> $\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$ <p><b>Standard Error of the Mean</b></p> $SE_{\bar{x}} = \frac{s}{\sqrt{n}}$	<p><b>Standard Deviation</b></p> $s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n - 1}}$ <p><b>Chi-Square</b></p> $\chi^2 = \sum \frac{(o - e)^2}{e}$																																			
<b>Chi-Square Table</b>																																				
<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th rowspan="2" style="padding: 2px;">p value</th> <th colspan="8" style="padding: 2px;">Degrees of Freedom</th> </tr> <tr> <th style="padding: 2px;">1</th> <th style="padding: 2px;">2</th> <th style="padding: 2px;">3</th> <th style="padding: 2px;">4</th> <th style="padding: 2px;">5</th> <th style="padding: 2px;">6</th> <th style="padding: 2px;">7</th> <th style="padding: 2px;">8</th> </tr> </thead> <tbody> <tr> <td style="padding: 2px;">0.05</td> <td style="padding: 2px;">3.84</td> <td style="padding: 2px;">5.99</td> <td style="padding: 2px;">7.81</td> <td style="padding: 2px;">9.49</td> <td style="padding: 2px;">11.07</td> <td style="padding: 2px;">12.59</td> <td style="padding: 2px;">14.07</td> <td style="padding: 2px;">15.51</td> </tr> <tr> <td style="padding: 2px;">0.01</td> <td style="padding: 2px;">6.63</td> <td style="padding: 2px;">9.21</td> <td style="padding: 2px;">11.34</td> <td style="padding: 2px;">13.28</td> <td style="padding: 2px;">15.09</td> <td style="padding: 2px;">16.81</td> <td style="padding: 2px;">18.48</td> <td style="padding: 2px;">20.09</td> </tr> </tbody> </table>	p value	Degrees of Freedom								1	2	3	4	5	6	7	8	0.05	3.84	5.99	7.81	9.49	11.07	12.59	14.07	15.51	0.01	6.63	9.21	11.34	13.28	15.09	16.81	18.48	20.09	<p><math>\bar{x}</math> = sample mean</p> <p><math>n</math> = sample size</p> <p><math>s</math> = sample standard deviation (i.e., the sample-based estimate of the standard deviation of the population)</p> <p><math>o</math> = observed results</p> <p><math>e</math> = expected results</p> <p><math>\Sigma</math> = sum of all</p> <p>Degrees of freedom are equal to the number of distinct possible outcomes minus one.</p>
p value		Degrees of Freedom																																		
	1	2	3	4	5	6	7	8																												
0.05	3.84	5.99	7.81	9.49	11.07	12.59	14.07	15.51																												
0.01	6.63	9.21	11.34	13.28	15.09	16.81	18.48	20.09																												
<p><b>Laws of Probability</b></p> <p>If A and B are mutually exclusive, then:</p> $P(A \text{ or } B) = P(A) + P(B)$ <p>If A and B are independent, then:</p> $P(A \text{ and } B) = P(A) \times P(B)$ <p><b>Hardy-Weinberg Equations</b></p> $p^2 + 2pq + q^2 = 1$ <p style="margin-left: 100px;"><math>p</math> = frequency of allele 1 in a population</p> $p + q = 1$ <p style="margin-left: 100px;"><math>q</math> = frequency of allele 2 in a population</p>	<p style="text-align: center;"><b>Metric Prefixes</b></p> <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 5px;"><b>Factor</b></th> <th style="text-align: left; padding: 5px;"><b>Prefix</b></th> <th style="text-align: left; padding: 5px;"><b>Symbol</b></th> </tr> </thead> <tbody> <tr><td style="padding: 5px;"><math>10^9</math></td><td style="padding: 5px;">giga</td><td style="padding: 5px;">G</td></tr> <tr><td style="padding: 5px;"><math>10^6</math></td><td style="padding: 5px;">mega</td><td style="padding: 5px;">M</td></tr> <tr><td style="padding: 5px;"><math>10^3</math></td><td style="padding: 5px;">kilo</td><td style="padding: 5px;">k</td></tr> <tr><td style="padding: 5px;"><math>10^{-1}</math></td><td style="padding: 5px;">deci</td><td style="padding: 5px;">d</td></tr> <tr><td style="padding: 5px;"><math>10^{-2}</math></td><td style="padding: 5px;">centi</td><td style="padding: 5px;">c</td></tr> <tr><td style="padding: 5px;"><math>10^{-3}</math></td><td style="padding: 5px;">milli</td><td style="padding: 5px;">m</td></tr> <tr><td style="padding: 5px;"><math>10^{-6}</math></td><td style="padding: 5px;">micro</td><td style="padding: 5px;"><math>\mu</math></td></tr> <tr><td style="padding: 5px;"><math>10^{-9}</math></td><td style="padding: 5px;">nano</td><td style="padding: 5px;">n</td></tr> <tr><td style="padding: 5px;"><math>10^{-12}</math></td><td style="padding: 5px;">pico</td><td style="padding: 5px;">p</td></tr> </tbody> </table>	<b>Factor</b>	<b>Prefix</b>	<b>Symbol</b>	$10^9$	giga	G	$10^6$	mega	M	$10^3$	kilo	k	$10^{-1}$	deci	d	$10^{-2}$	centi	c	$10^{-3}$	milli	m	$10^{-6}$	micro	$\mu$	$10^{-9}$	nano	n	$10^{-12}$	pico	p					
<b>Factor</b>	<b>Prefix</b>	<b>Symbol</b>																																		
$10^9$	giga	G																																		
$10^6$	mega	M																																		
$10^3$	kilo	k																																		
$10^{-1}$	deci	d																																		
$10^{-2}$	centi	c																																		
$10^{-3}$	milli	m																																		
$10^{-6}$	micro	$\mu$																																		
$10^{-9}$	nano	n																																		
$10^{-12}$	pico	p																																		
<p>Mode = value that occurs most frequently in a data set</p> <p>Median = middle value that separates the greater and lesser halves of a data set</p> <p>Mean = sum of all data points divided by number of data points</p> <p>Range = value obtained by subtracting the smallest observation (sample minimum) from the greatest (sample maximum)</p>																																				

<b>Rate and Growth</b>		<b>Water Potential ( <math>\Psi</math> )</b>
<p><b>Rate</b>  <math>\frac{dY}{dt}</math></p> <p><b>Population Growth</b>  <math>\frac{dN}{dt} = B - D</math></p> <p><b>Exponential Growth</b>  <math>\frac{dN}{dt} = r_{\max} N</math></p> <p><b>Logistic Growth</b>  <math>\frac{dN}{dt} = r_{\max} N \left( \frac{K - N}{K} \right)</math></p>	<p><math>dY</math> = amount of change  <math>dt</math> = change in time</p> <p><math>B</math> = birth rate  <math>D</math> = death rate  <math>N</math> = population size  <math>K</math> = carrying capacity  <math>r_{\max}</math> = maximum per capita growth rate of population</p>	<p><math>\Psi = \Psi_p + \Psi_s</math></p> <p><math>\Psi_p</math> = pressure potential  <math>\Psi_s</math> = solute potential</p> <p>The water potential will be equal to the solute potential of a solution in an open container because the pressure potential of the solution in an open container is zero.</p> <p><b>The Solute Potential of a Solution</b>  <math>\Psi_s = -iCRT</math></p> <p><math>i</math> = ionization constant (1.0 for sucrose because sucrose does not ionize in water)  <math>C</math> = molar concentration  <math>R</math> = pressure constant  (<math>R = 0.0831</math> liter bars/mole K)  <math>T</math> = temperature in Kelvin (<math>^{\circ}\text{C} + 273</math>)</p>
<p><b>Simpson's Diversity Index</b>  Diversity Index = <math>1 - \sum \left( \frac{n}{N} \right)^2</math>  <math>n</math> = total number of organisms of a particular species  <math>N</math> = total number of organisms of all species</p>		<p><b>pH</b> = <math>-\log[\text{H}^+]</math></p>
<b>Surface Area and Volume</b>		
<p><b>Surface Area of a Sphere</b>  <math>SA = 4\pi r^2</math></p> <p><b>Surface Area of a Rectangular Solid</b>  <math>SA = 2lh + 2lw + 2wh</math></p> <p><b>Surface Area of a Cylinder</b>  <math>SA = 2\pi rh + 2\pi r^2</math></p> <p><b>Surface Area of a Cube</b>  <math>SA = 6s^2</math></p>	<p><b>Volume of a Sphere</b>  <math>V = \frac{4}{3}\pi r^3</math></p> <p><b>Volume of a Rectangular Solid</b>  <math>V = lwh</math></p> <p><b>Volume of a Cylinder</b>  <math>V = \pi r^2 h</math></p> <p><b>Volume of a Cube</b>  <math>V = s^3</math></p>	<p><math>r</math> = radius  <math>l</math> = length  <math>h</math> = height  <math>w</math> = width  <math>s</math> = length of one side of a cube  <math>SA</math> = surface area  <math>V</math> = volume</p>